

# Introduction to cryptographic protocols

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(Slides by Stéphanie Delaune)



## Cryptographic protocols

- small programs designed to **secure** communication (various security goals)
- use **cryptographic primitives** (e.g. encryption, hash function,

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# Security properties (1)

- **Secrecy**: May an intruder learn some secret message between two honest participants?
- **Authentication**: Is the agent **Alice** really talking to **Bob**?
- **Fairness**: **Alice** and **Bob** want to sign a contract. **Alice** initiates the protocol. May **Bob** obtain some advantage?
- **Non-repudiation**: **Alice** sends a message to **Bob**. **Alice** cannot later deny having sent this message. **Bob** cannot deny having received the message.
- ...

## Security properties: E-voting (2)



**Eligibility:** only legitimate voters can vote, and only once

**Fairness:** no early results can be obtained which could influence the remaining voters

### Individual verifiability:

a voter can verify that her vote was really counted

### Universal verifiability:

the published outcome really is the sum of all the votes



Belgique - Election 2004 - <http://www.poueva.be/> - (C) Kanar

## Security properties: E-voting (3)

**Privacy:** the fact that a particular voted in a particular way is not revealed to anyone



**Receipt-freeness:** a voter cannot prove that she voted in a certain way (this is important to protect voters from coercion)

**Coercion-resistance:** same as receipt-freeness, but the coercer interacts with the voter during the protocol, (e.g. by preparing messages)

## Cryptographic primitives

Algorithms that are frequently used to build computer security systems. These routines include, but are not limited to, **encryption** and **signature** functions.

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### Symmetric encryption



→ **Examples:** Caesar encryption, DES, AES, ...



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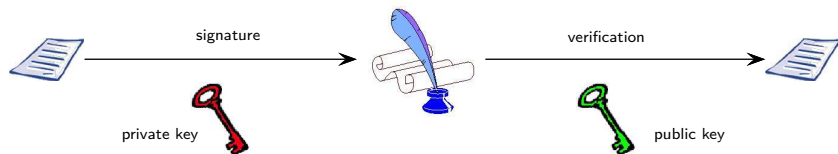
### Asymmetric encryption



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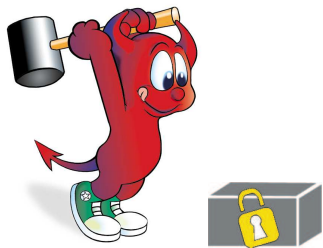
### Signature



# Security of cryptographic protocols

How cryptographic protocols can be attacked?

Breaking encryption



cryptanalysis

Logical attack



replay attacks

man-in-the-middle attacks

# Replay attacks



transfer 100 euros into  
the merchant's account

---



# Replay attacks



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**Example:** attack on the decoders (TV)

→ block the message that cancels the subscription

## Symbolic approach

- **messages** are represented by **terms** rather than bit-strings
  - ↔  $\{m\}_k$  encryption of the message  $m$  with key  $k$ ,
  - ↔  $\langle m_1, m_2 \rangle$  pairing of messages  $m_1$  and  $m_2$ , ...
- **attacker** controls the network and can perform **specific actions**



# Logical attacks - How to detect them?

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## Relevance of the approach

- **numerous** attacks have already been obtained,
- **soundness results** w.r.t. to the **computational model** already exist, e.g. [Abadi & Rogaway'01]
- allows us to perform **automatic** verification



## Credit Card Payment Protocol



# Example: credit card payment



- The client  $C$  puts his credit card  $C$  in the terminal  $T$ .
- The merchant enters the amount  $M$  of the sale.
- The terminal authenticates the credit card.
- The client enters his PIN.  
If  $M \geq 100\text{€}$ , then in 20% of cases,
  - The terminal contacts the bank  $B$ .
  - The banks gives its authorisation.



the Bank  $B$  , the Client  $Cl$ , the Credit Card  $C$  and the Terminal  $T$

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## Bank

- a **private** signature key –  $\text{priv}(B)$
- a **public** key to verify a signature –  $\text{pub}(B)$
- a **secret** key shared with the credit card –  $K_{CB}$

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## Credit Card

- some **Data**: name of the cardholder, expiry date ...
- a signature of the **Data** –  $\{\text{hash}(\text{Data})\}_{\text{priv}(B)}$
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## Terminal

- the **public** key of the bank –  $\text{pub}(B)$

# Payment protocol

the terminal  $T$  reads the credit card  $C$ :

1.  $C \rightarrow T : Data, \{hash(Data)\}_{priv(B)}$



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the terminal  $T$  reads the credit card  $C$ :

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the terminal  $T$  asks the code:

2.  $T \rightarrow CI : \text{code?}$
3.  $CI \rightarrow C : 1234$
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4.  $C \rightarrow T$  :  $ok$

the terminal  $T$  requests authorisation the bank  $B$ :

5.  $T \rightarrow B$  :  $auth?$

6.  $B \rightarrow T$  : 4528965874123

7.  $T \rightarrow C$  : 4528965874123

8.  $C \rightarrow T$  :  $\{4528965874123\}_{K_{CB}}$

9.  $T \rightarrow B$  :  $\{4528965874123\}_{K_{CB}}$

10.  $B \rightarrow T$  :  $ok$

# Attack against credit cards

Initially, security was guaranteed by:

- cards hard to replicate,
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However, there are attacks!

- **cryptographic** attack: 320-bit keys are no longer secure,
- **logical** attack: no link between the 4-digit PIN code and the authentication,
- **hardware** attack: replication of cards.



→ “YesCard” made by Serge Humpich (1997).

# The « YesCard »: how does it work?

## Logical attack

1.  $C \rightarrow T : \text{Data}, \{\text{hash}(\text{Data})\}_{\text{priv}(B)}$

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**Remark:** there is always somebody to debit.

→ add a fake ciphertext on a fake card (Serge Humpich).

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1.  $C' \rightarrow T$  :  $\text{XXX}, \{\text{hash}(\text{XXX})\}_{\text{priv}(B)}$
2.  $T \rightarrow CI$  :  $PIN?$
3.  $CI \rightarrow C'$  :  $0000$
4.  $C' \rightarrow T$  :  $ok$



# Needham-Schroeder (public-key) Protocol

# Needham-Schroeder's Protocol (1978)



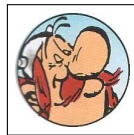
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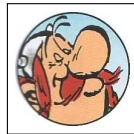
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## Questions

- Is  $N_b$  secret between  $A$  and  $B$  ?
- When  $B$  receives  $\{N_b\}_{\text{pub}(B)}$ , does this message really comes from  $A$  ?

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## Attack

An attack was found 17 years after its publication! [Lowe 96]

# Example: Man in the middle attack



Agent A



Intruder I



Agent B

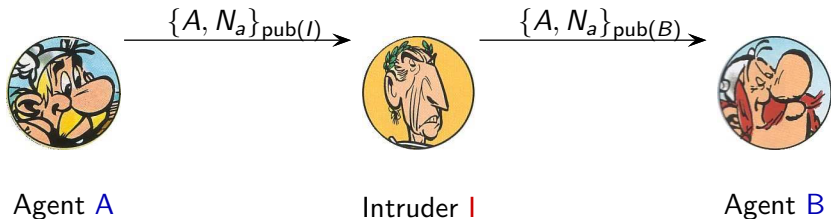
## Attack

- involving 2 sessions in **parallel**,
- an **honest** agent has to **initiate** a session with **I**.

$$\begin{aligned} A \rightarrow B & : \{A, N_a\}_{\text{pub}(B)} \\ B \rightarrow A & : \{N_a, N_b\}_{\text{pub}(A)} \\ A \rightarrow B & : \{N_b\}_{\text{pub}(B)} \end{aligned}$$

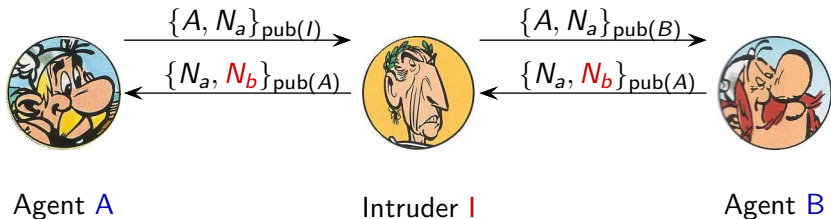


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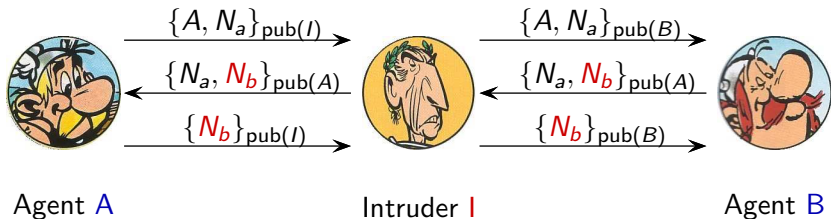
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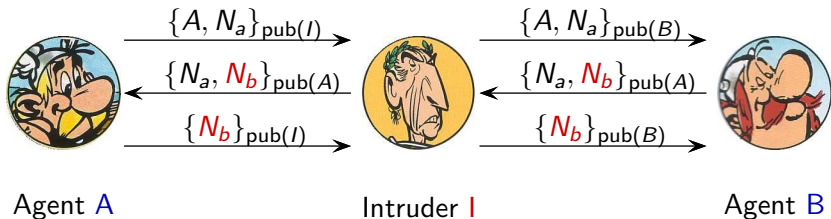
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# Example: Man in the middle attack



## Attack

- the intruder knows  $N_b$ ,
- When B finishes his session (apparently with A), A has never talked with B.

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 $B \rightarrow A : \{N_a, N_b\}_{\text{pub}(A)}$   
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